

Strokovno izobraževanje

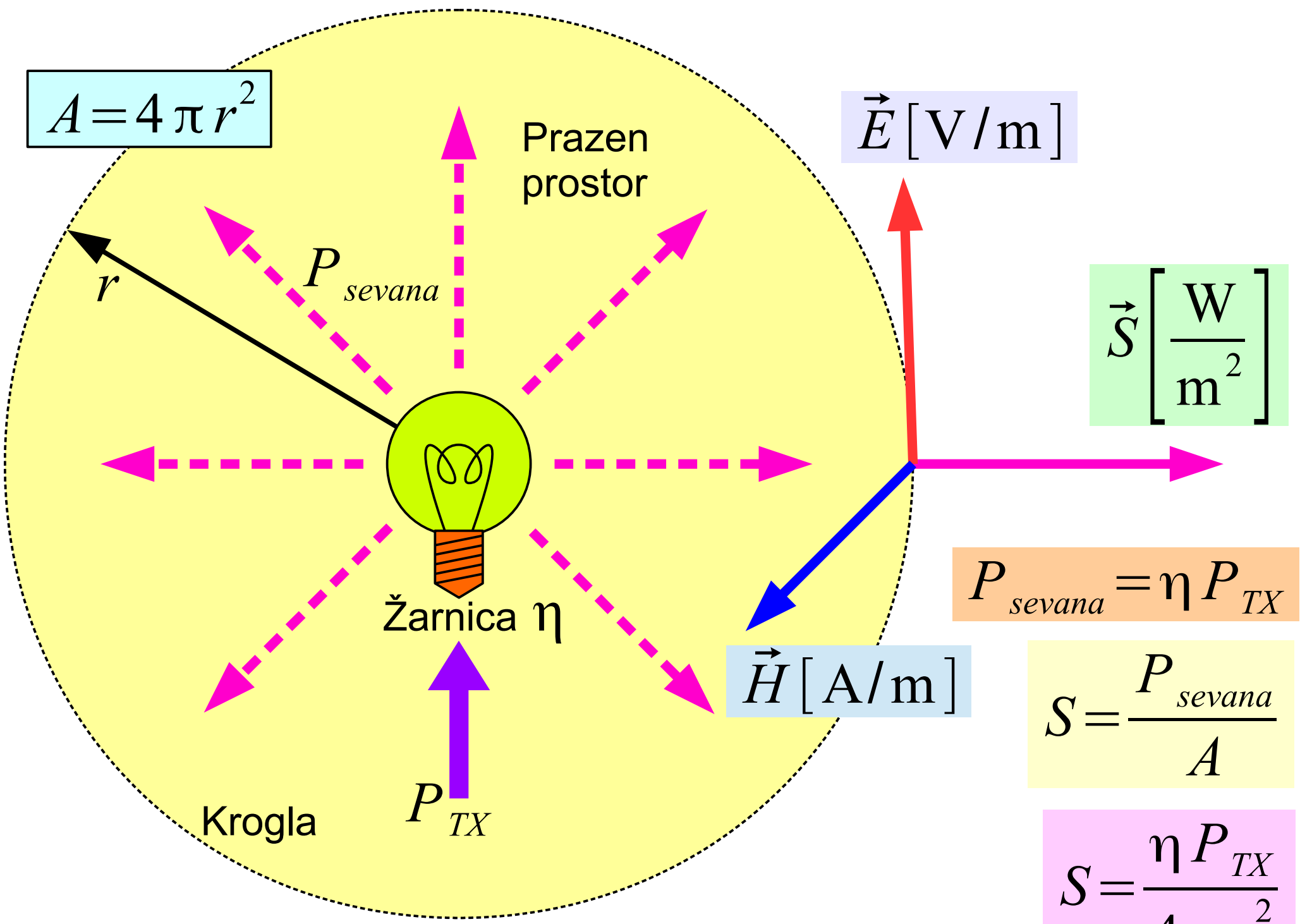
# ELEKTROMAGNETNO SEVANJE

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AKOS, Ljubljana, 22.5.2015

## Seznam prosojnic predavanja: ELEKTROMAGNETNO SEVANJE

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$$A = 4\pi r^2$$

$$\vec{E} \text{ [V/m]}$$

$$\vec{S} \left[ \frac{\text{W}}{\text{m}^2} \right]$$

$$P_{sevana} = \eta P_{TX}$$

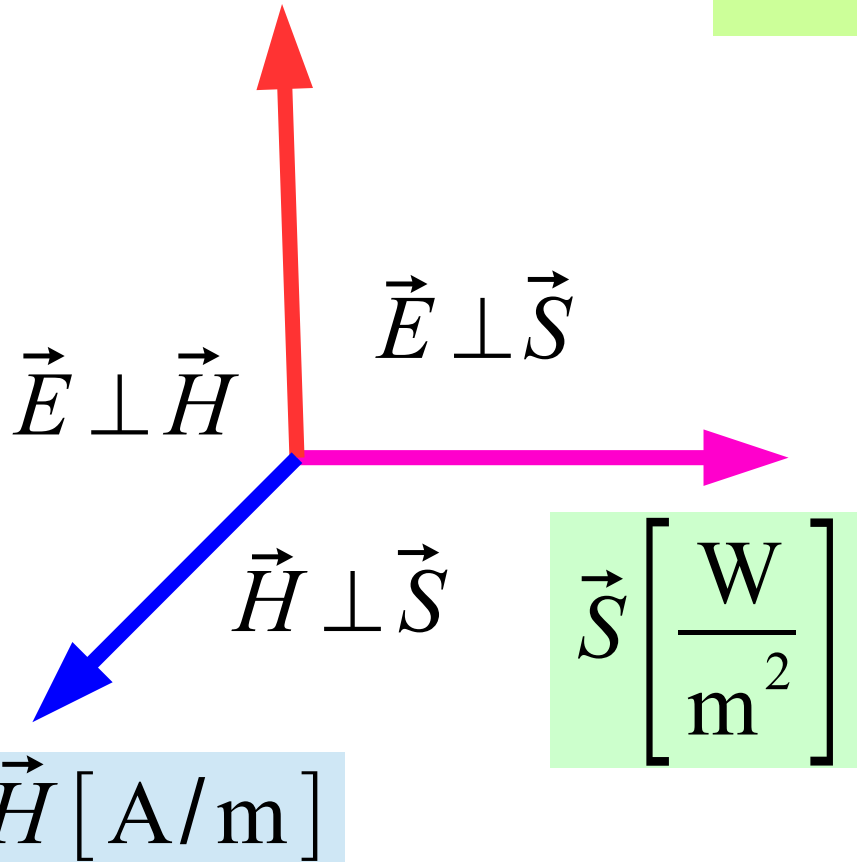
$$S = \frac{P_{sevana}}{A}$$

$$S = \frac{\eta P_{TX}}{4\pi r^2}$$

1 - Sevanje neusmerjenega vira

$$\vec{E} \text{ [V/m]}$$

$$\text{Sevanje: } \frac{E}{H} = Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}} \approx 377 \Omega$$



$$\vec{S} = \frac{1}{2} \vec{E} \times \vec{H}^*$$

Vršne  
vrednosti  
polja

$$S = \frac{|\vec{E}|^2}{2Z_0}$$

$$E = \sqrt{2Z_0 S}$$

$$\vec{S} = \vec{E}_{eff} \times \vec{H}_{eff}^*$$

Efektivne  
vrednosti  
polja

$$S = \frac{|\vec{E}_{eff}|^2}{Z_0}$$

$$E_{eff} = \sqrt{Z_0 S}$$

*Prazen prostor  $\mu_0, \epsilon_0$   
brez izgub!*

Smernost  $D = \frac{4\pi}{\Omega}$

Žaromet  $D$

Žarnica  $\eta$

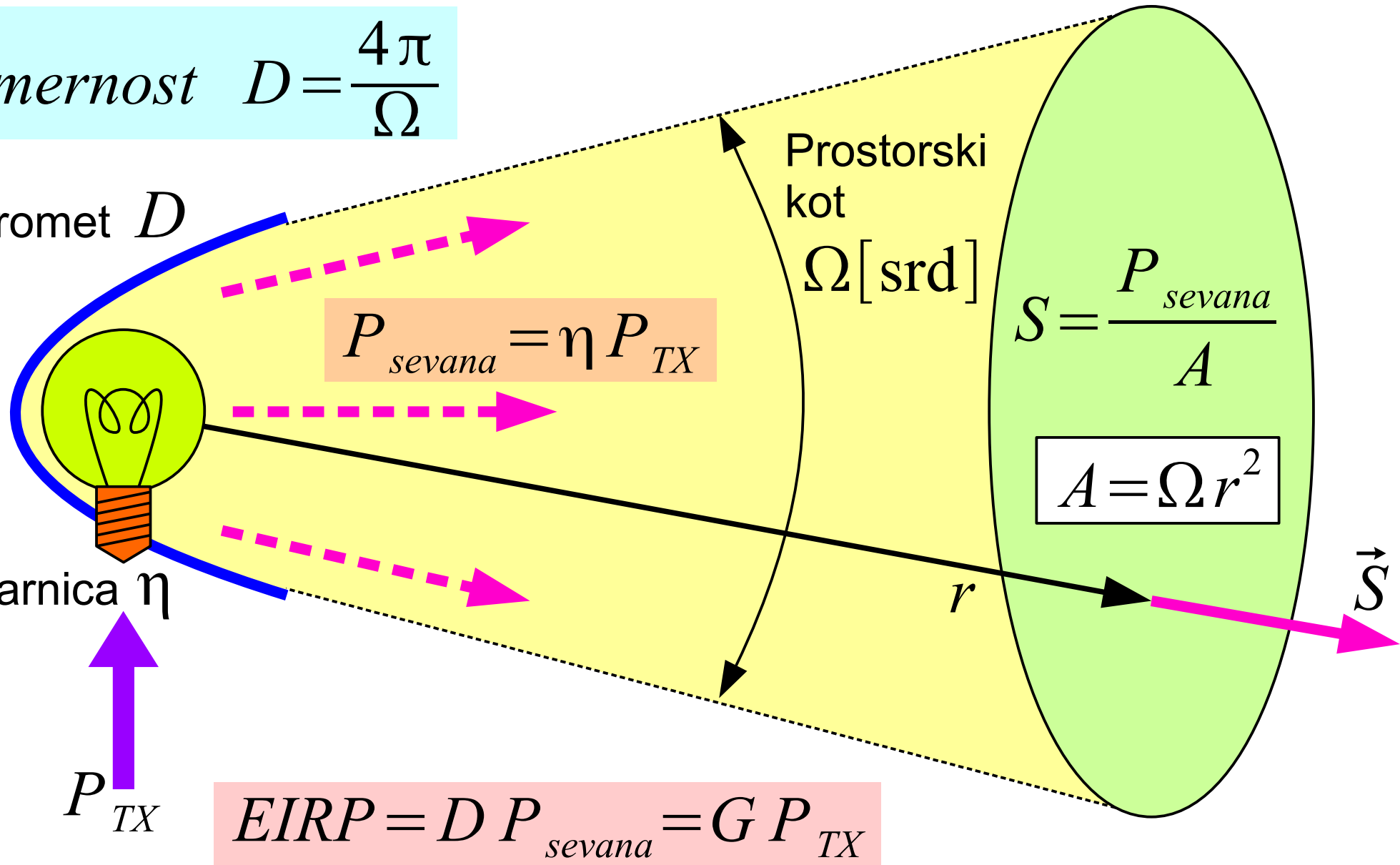
$P_{TX}$

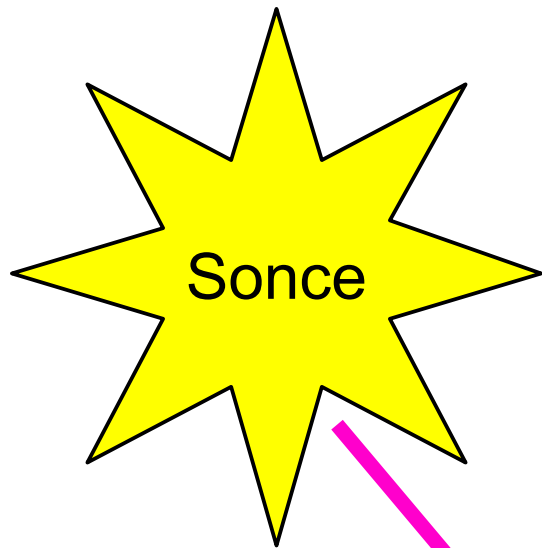
$EIRP = D P_{sevana} = G P_{TX}$

Dobitek  $G = \eta D$

3 - Sevanje usmerjenega izvora

$$S = \frac{\eta P_{TX}}{\Omega r^2} = \frac{\eta D P_{TX}}{4\pi r^2} = \frac{G P_{TX}}{4\pi r^2}$$





Učinek sevanja	Gostota pretoka moči $S$		Poljska jakost $E_{eff}$
Sončna svetloba	1kW/m <sup>2</sup>	100mW/cm <sup>2</sup>	614V <sub>eff</sub> /m
Zaznaven učinek	100W/m <sup>2</sup>	10mW/cm <sup>2</sup>	194V <sub>eff</sub> /m
Varna meja	10W/m <sup>2</sup>	1mW/cm <sup>2</sup>	61V <sub>eff</sub> /m
Zakonska omejitev	0.1W/m <sup>2</sup>	10μW/cm <sup>2</sup>	6V <sub>eff</sub> /m

$$S = 1 \text{ kW/m}^2$$

(na površini Zemlje)

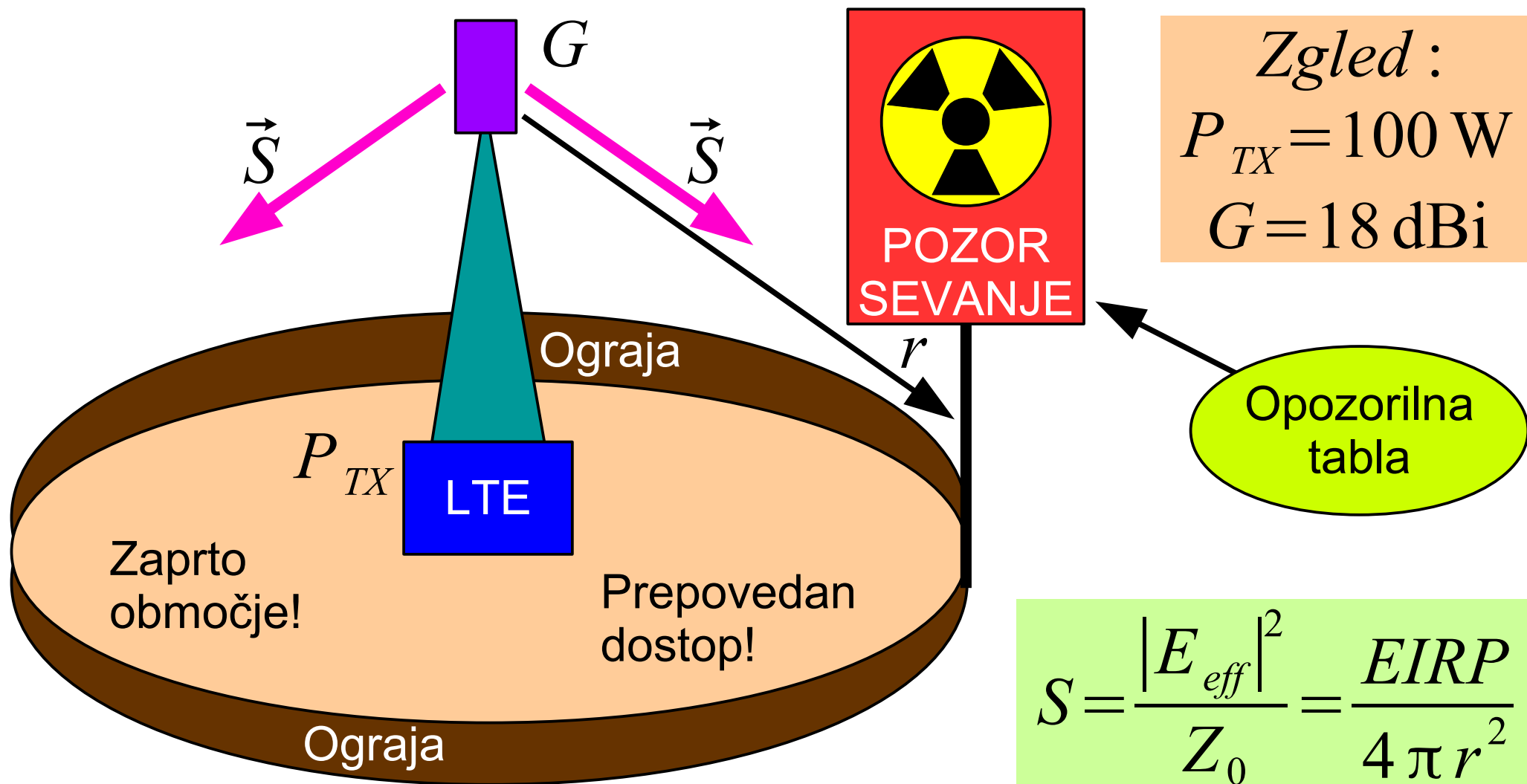
$$P_{RX} = S \cdot A_{maček}$$

$$A_{maček} = 0.05 \text{ m}^2$$



$$P_{RX} = 50 \text{ W}$$

$$EIRP = +68 \text{ dBm} = 10^{(68/10)} \cdot 1 \text{ mW} = 6.3 \text{ kW}$$



$$S = \frac{|E_{eff}|^2}{Z_0} = \frac{EIRP}{4\pi r^2}$$

*EU zakonodaja*

$$E_{eff} \leq 6 \text{ V}_{eff} / \text{m}$$

5 - Ograja okoli vira sevanja

$$r \geq \sqrt{\frac{Z_0 EIRP}{4\pi |E_{eff}|^2}} = 72.5 \text{ m}$$

Smernost  $D = \frac{4\pi}{\Omega}$

Žaromet  $D$

Žarnica  $\eta_{TX}$

$P_{TX}$

$P_{sevana} = \eta_{TX} P_{TX}$

Dobitek  $G = \eta_{TX} D$

Prostorski kot  $\Omega$

$A > A_{RX}$

$A_{RX}$   
 $\eta_{RX}$

$P_{RX}$

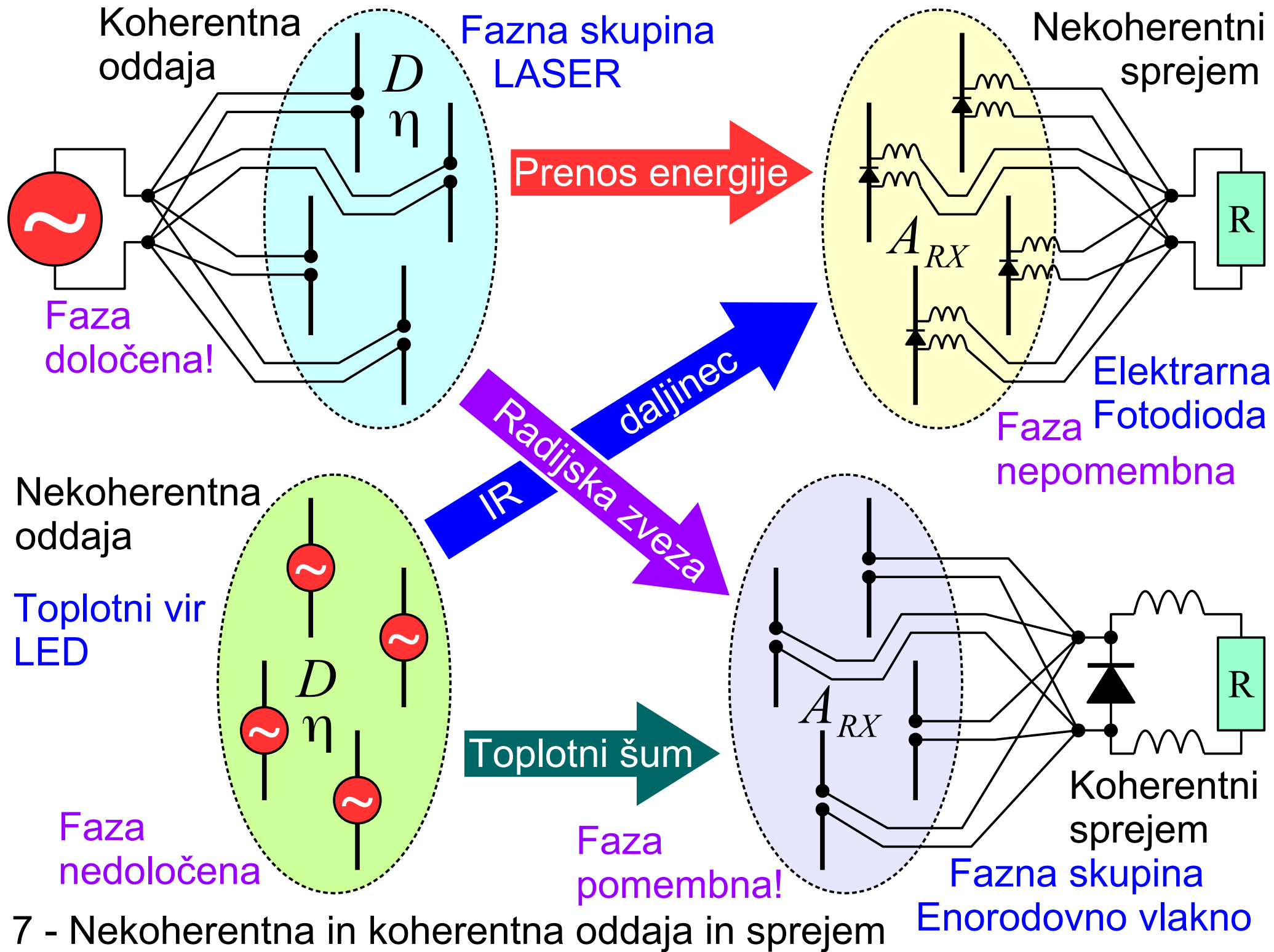
$r$

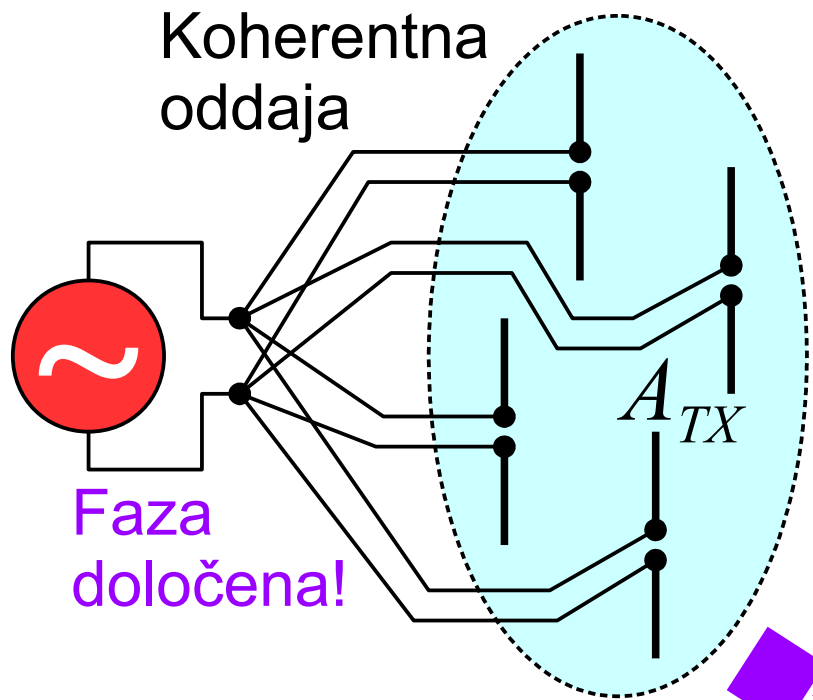
$\vec{S}$

$$P_{RX} = A_{RX} \eta_{RX} S = \frac{A_{RX} \eta_{RX} \eta_{TX} D P_{TX}}{4\pi r^2} = P_{TX} \cdot \frac{A_{RX} \eta_{RX} G}{4\pi r^2}$$

6 - Domet brezvrvične zveze v praznem prostoru







$$D_{TX} \quad A_{effTX} = \frac{\lambda^2}{4\pi} \cdot D_{TX}$$

$$G_{TX} \quad A_{effTX} = \frac{\lambda^2}{4\pi} \cdot \frac{G_{TX}}{\eta_{TX}}$$

$$A_{eff} = A \cdot \eta_o \equiv \text{efektivna površina}$$

$$\eta_o \equiv \text{izkoristek osvetlitve}$$

$$\eta_o \approx 50\% \dots 80\%$$

Radijska zveza

$$D_{RX} = \frac{4\pi}{\lambda^2} \cdot A_{effRX}$$

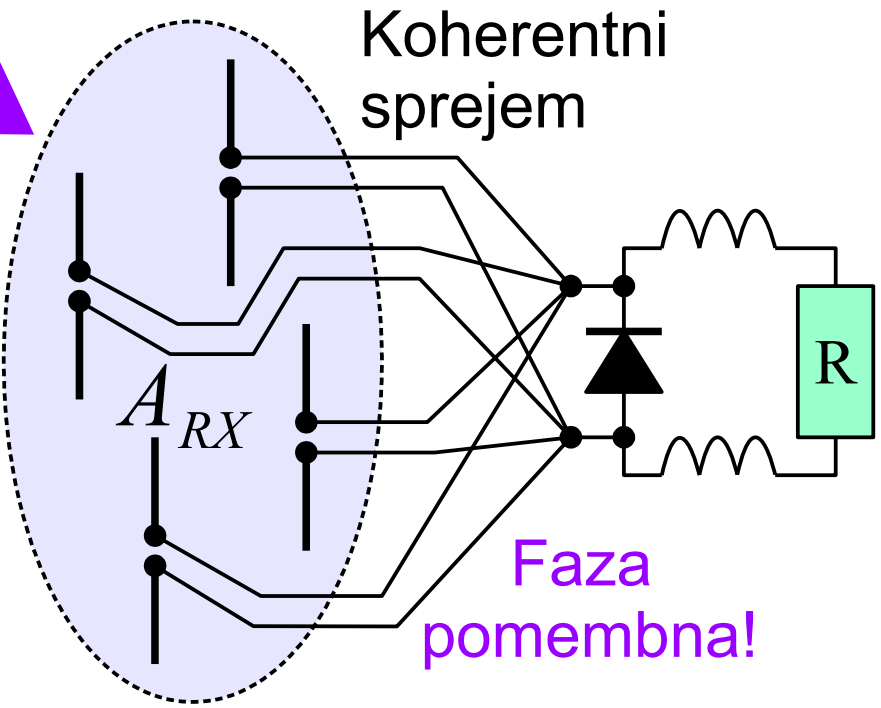
$$G_{RX} = \frac{4\pi}{\lambda^2} \cdot A_{effRX} \cdot \eta_{RX}$$

$$A_{effRX}$$

$$\eta_{RX}$$

$$D_{RX}$$

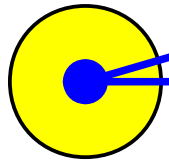
$$G_{RX}$$



8 - Efektivna površina koherentne antene

$$\Delta l \approx d^2 / 8r$$

Točkasti vir sevanja

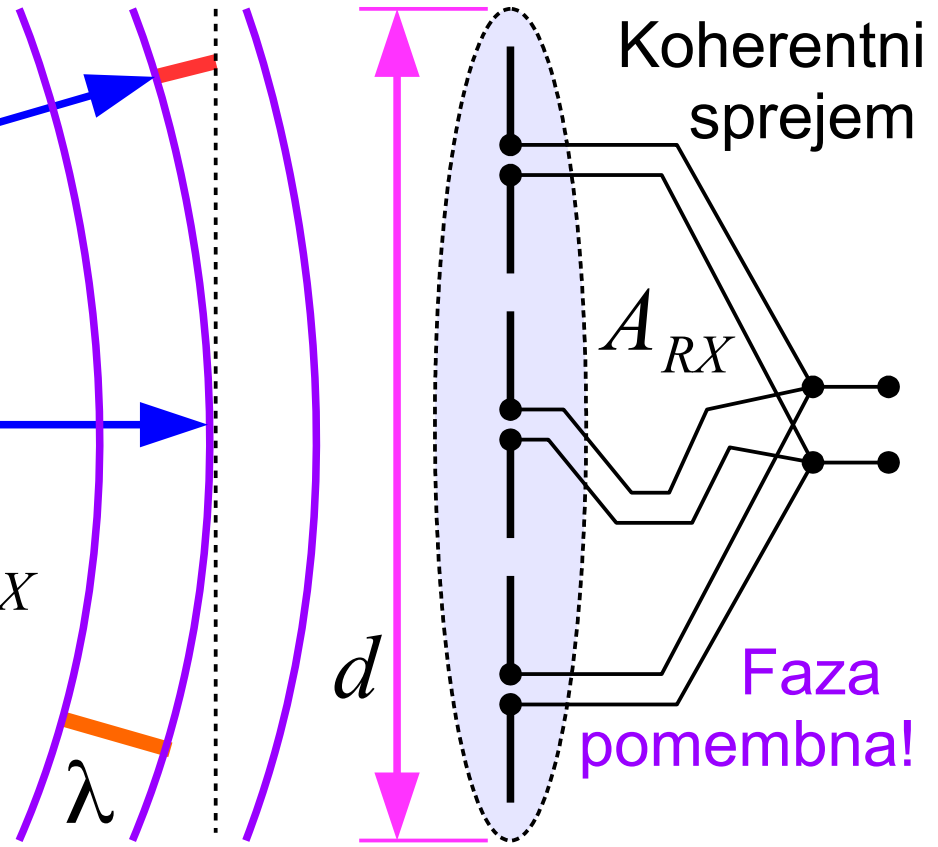


$r + \Delta l$

$r \gg d$

Pogoj faze stroži od amplitude  $A > A_{RX}$

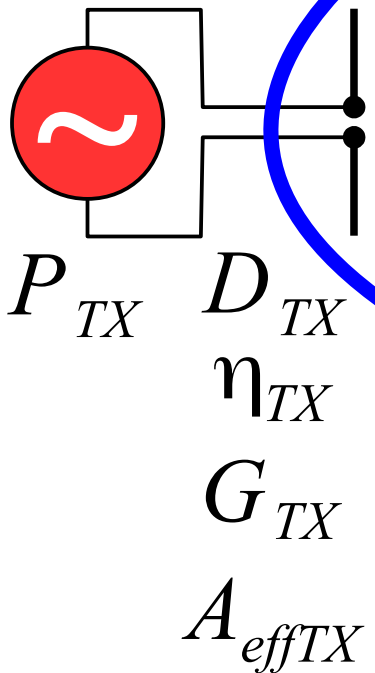
$$\Delta P_{dB} \approx 20 \log_{10} \frac{\sin \Delta \phi / 2}{\Delta \phi / 2}$$



$\Delta l$	$\Delta \phi$ [rd]	$\Delta P$ [dB]	$r \geq$	Uporaba
$\lambda/2$	$\pi$	-3.922	$d^2/4\lambda$	Globinska ostrina fotoaparata
$\lambda/4$	$\pi/2$	-0.912	$d^2/2\lambda$	Lord Rayleigh 1891
$\lambda/8$	$\pi/4$	-0.224	$d^2/\lambda$	
$\lambda/16$	$\pi/8$	-0.056	$2d^2/\lambda$	Meritev radijskih signalov

9 - Fraunhoferjev pogoj (Rayleighjeva razdalja)

Koherentna oddaja

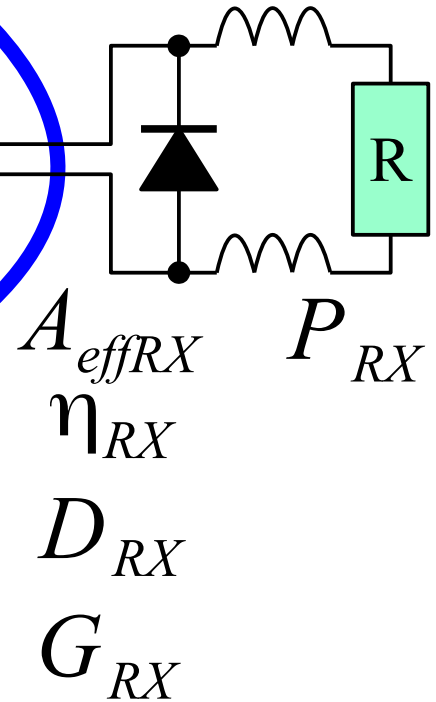


$$r \geq \frac{2d_{TX}^2}{\lambda} + \frac{2d_{RX}^2}{\lambda}$$

Prazen prostor

Harald Friis 1945

Koherentni sprejem



$$P_{RX} = P_{TX} \frac{\eta_{TX} D_{TX} A_{effRX} \eta_{RX}}{4\pi r^2}$$

Zapis z dobitki anten:

$$P_{RX} = P_{TX} G_{TX} G_{RX} \left( \frac{\lambda}{4\pi r} \right)^2$$

**Recipročnost!**

Zapis s površinami anten:

$$P_{RX} = P_{TX} \frac{\eta_{TX} A_{effTX} A_{effRX} \eta_{RX}}{\lambda^2 r^2}$$

$$D [\text{dBi}] = 10 \log_{10} D$$

$$G [\text{dBi}] = 10 \log_{10} G$$

dBi  $\equiv$  dB glede na neusmerjen (izotropni) vir

$$D [\text{dBd}] = D [\text{dBi}] - 2.15 \text{ dB}$$

$$G [\text{dBd}] = G [\text{dBi}] - 2.15 \text{ dB}$$

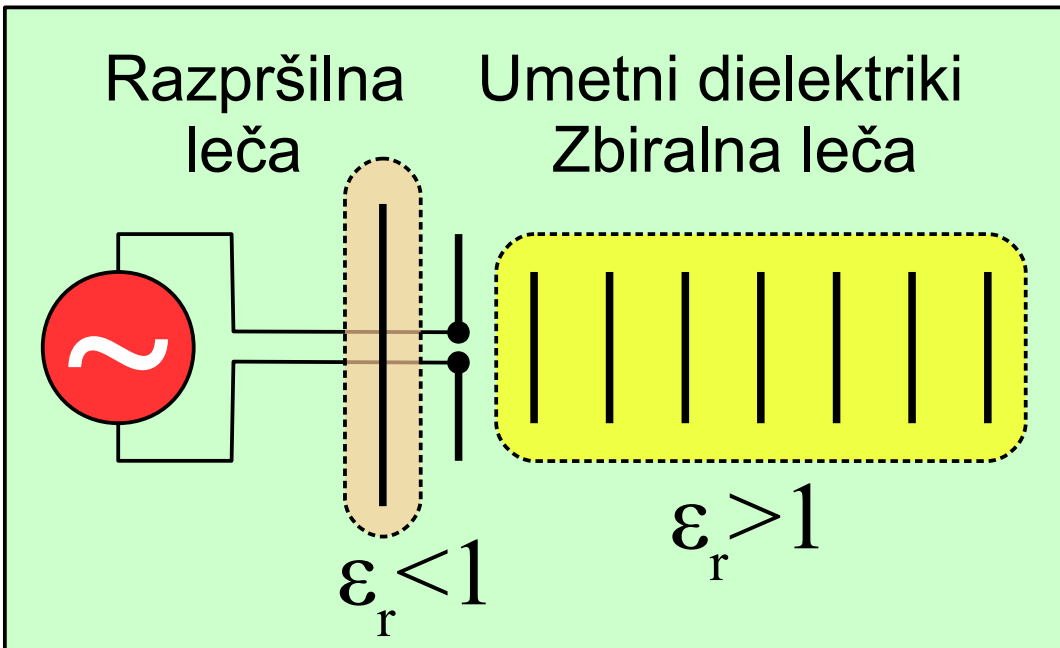
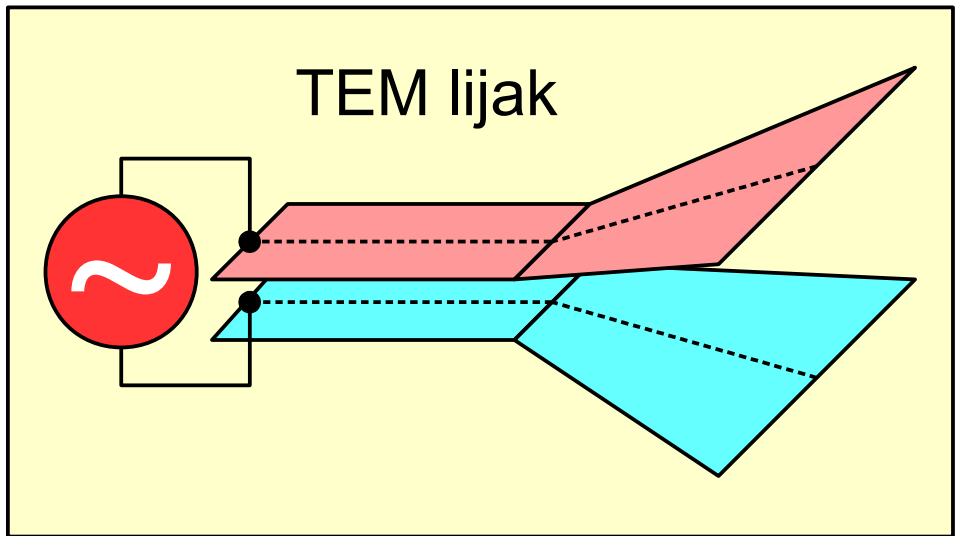
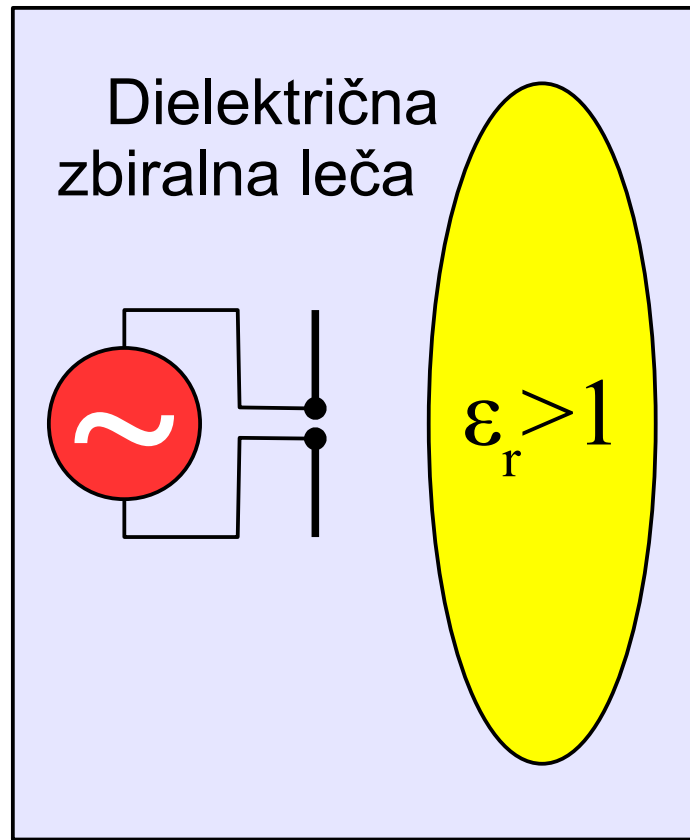
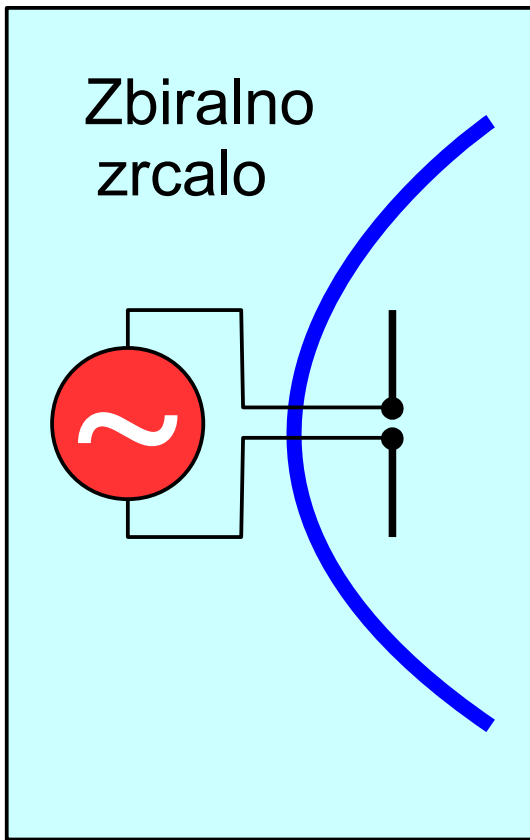
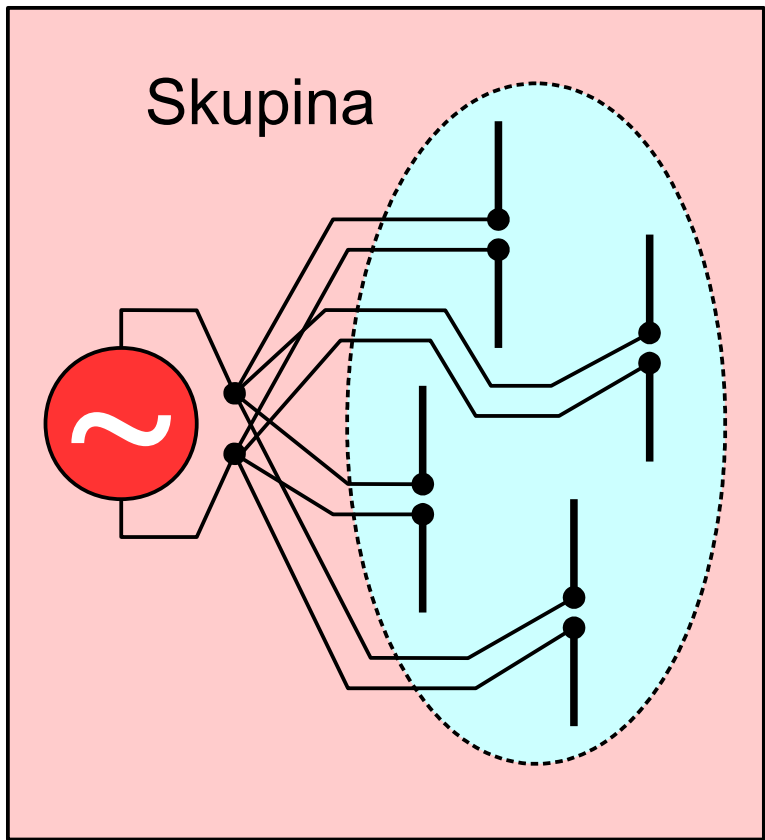
dBd  $\equiv$  dB glede na polvalni dipol

*Iskanje nesreče s Friisovo enačbo na tisoč in en način:*

$$P_{RX} [\text{dBm}] = P_{TX} [\text{dBm}] + G_{TX} [\text{dBi}] + G_{RX} [\text{dBi}] + \\ + 20 \log_{10} \lambda [\text{m}] - 20 \log_{10} r [\text{m}] - 21.98 \text{ dB}$$

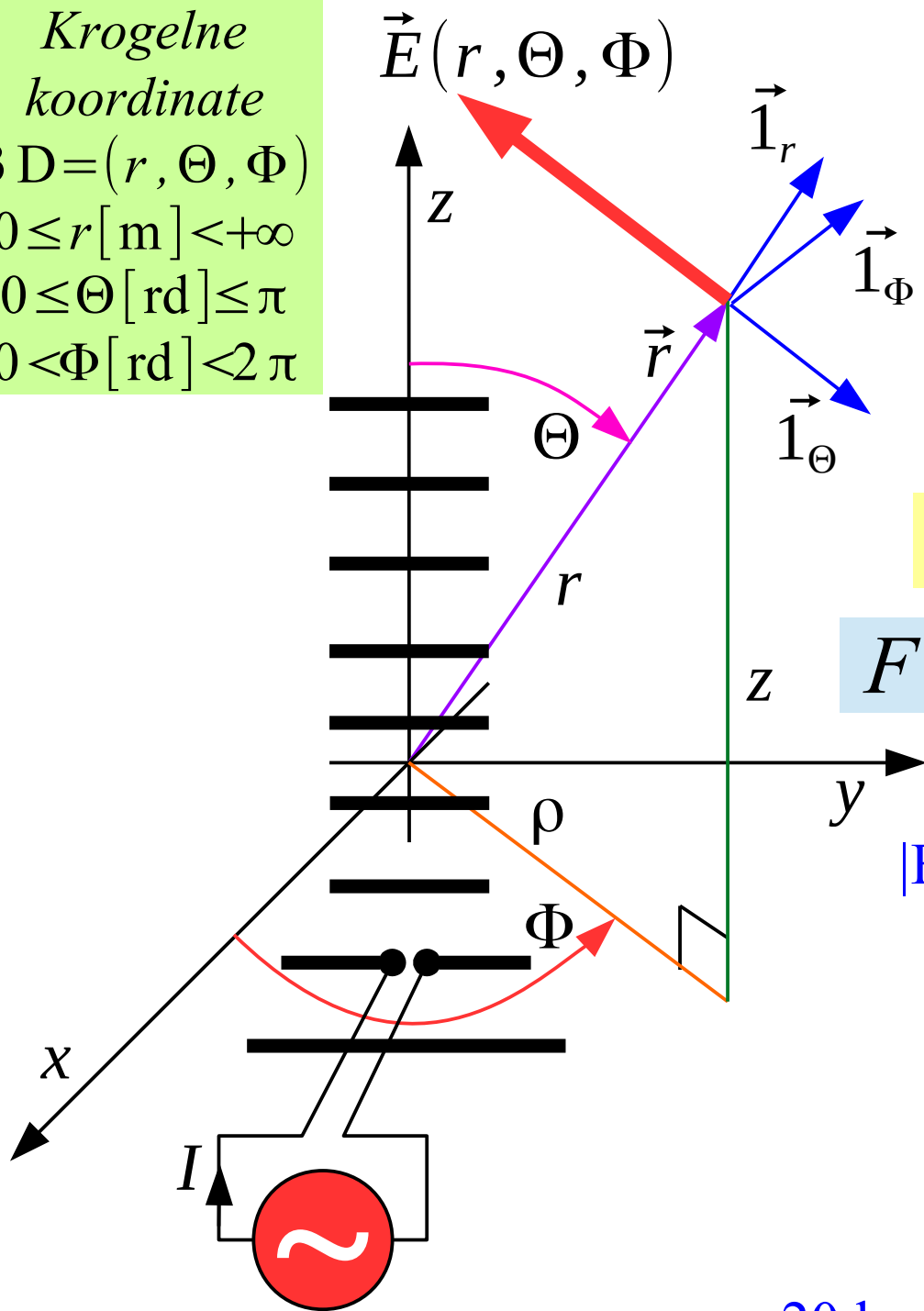
$$\lambda [\text{m}] \approx 299.7 / f [\text{MHz}] \quad \text{zrak: } n = 1.0003$$

$$P_{RX} [\text{dBm}] = P_{TX} [\text{dBm}] + G_{TX} [\text{dBi}] + G_{RX} [\text{dBi}] - \\ - 20 \log_{10} f [\text{MHz}] - 20 \log_{10} r [\text{m}] + 27.55 \text{ dB}$$



12 - Izvedbe usmerjenih anten

*Krogelne  
koordinata*  
 $3D = (r, \Theta, \Phi)$   
 $0 \leq r [\text{m}] < +\infty$   
 $0 \leq \Theta [\text{rd}] \leq \pi$   
 $0 < \Phi [\text{rd}] < 2\pi$



$$\vec{E} = \vec{1}_p \alpha I \frac{e^{-j2\pi \frac{r}{\lambda}}}{r} F(\Theta, \Phi)$$

$\vec{1}_p \equiv$  polarizacija

$F(\theta, \Phi) \equiv$  amplitudni smerni diagram

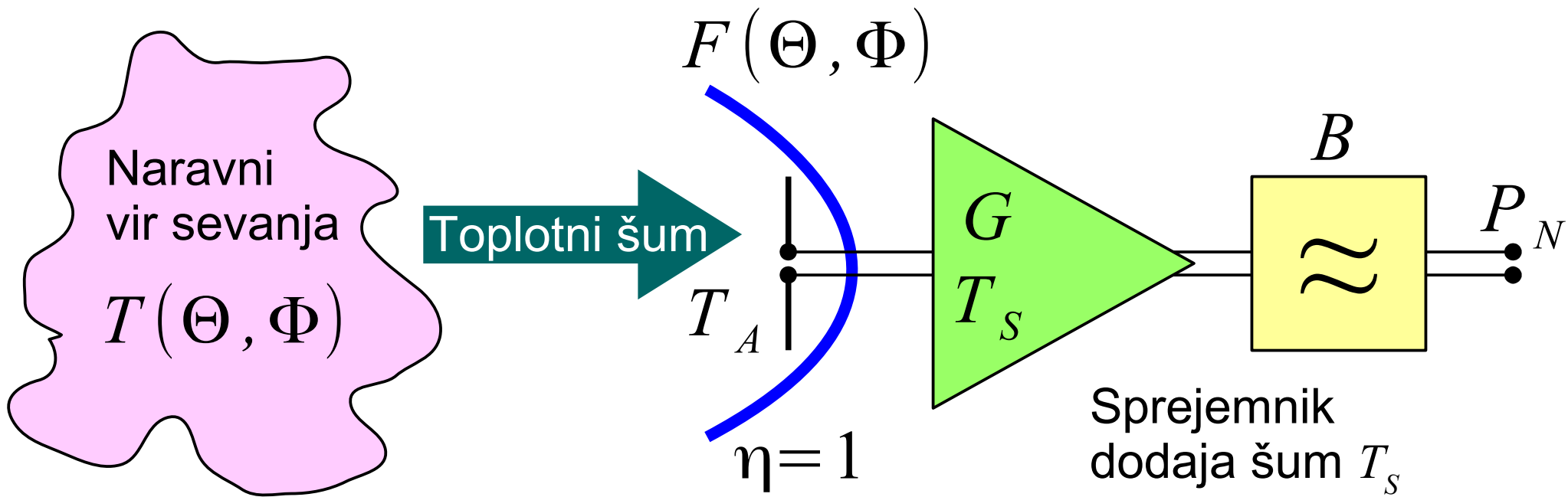
$F(\Theta, \Phi = 0) \equiv$  Ravnina H

$F(\Theta, \Phi = \pi/2) \equiv$  Ravnina E

$|F(\theta, \Phi)|^2 \equiv$  močnostni smerni diagram

$$D = \frac{4\pi |F(\Theta_{MAX}, \Phi_{MAX})|^2}{\oint\oint_{4\pi} |F(\Theta, \Phi)|^2 d\Omega}$$

$20 \log|F(\theta, \Phi)| \equiv$  decibelski smerni diagram



Vir dodaja šum  $T_A$

Brezizgubna antena  
ne dodaja šuma!

Sprejemnik  
dodaja šum  $T_S$

Boltzmannova konstanta  
za toplotni šum:

$$k_B \approx 1.38 \cdot 10^{-23} \text{ J/K}$$

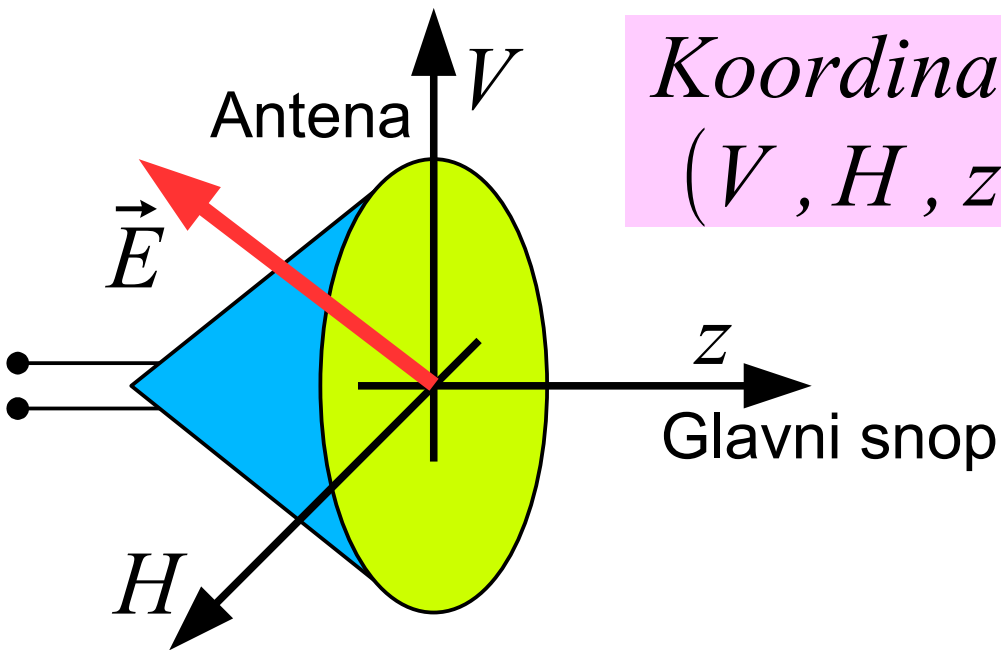
Moč šuma na  
izhodu sprejemnika:

$$P_N = G \cdot B \cdot k_B \cdot (T_A + T_S)$$

$$T_A = \frac{\iint_{4\pi} T(\Theta, \Phi) |F(\Theta, \Phi)|^2 d\Omega}{\iint_{4\pi} |F(\Theta, \Phi)|^2 d\Omega}$$

$T_A \equiv$  utežena vsota šuma  $T(\Theta, \Phi)$





*Koordinate*  
( $V, H, z$ )

*Linearne komponente:*

$$E_V = \vec{E} \cdot \vec{1}_V$$

$$E_H = \vec{E} \cdot \vec{1}_H$$

*Krožne komponente:*

$$E_L = \vec{E} \cdot \vec{1}_L^*$$

$$E_D = \vec{E} \cdot \vec{1}_D^*$$

Prečno valovanje: dve neodvisni polarizaciji!

*Krožni smerniki:*

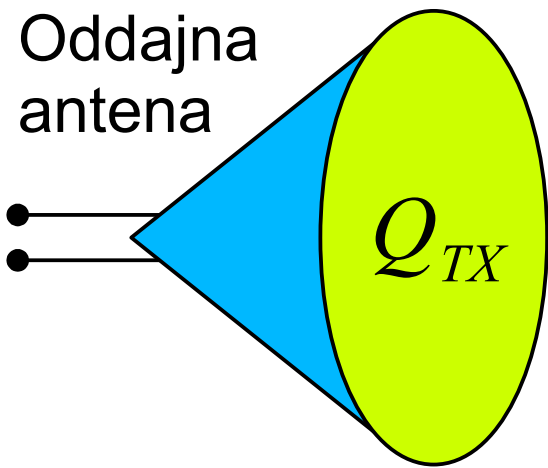
$$\vec{1}_L = \frac{\vec{1}_V + j\vec{1}_H}{\sqrt{2}}$$

$$\vec{1}_D = \frac{\vec{1}_V - j\vec{1}_H}{\sqrt{2}}$$

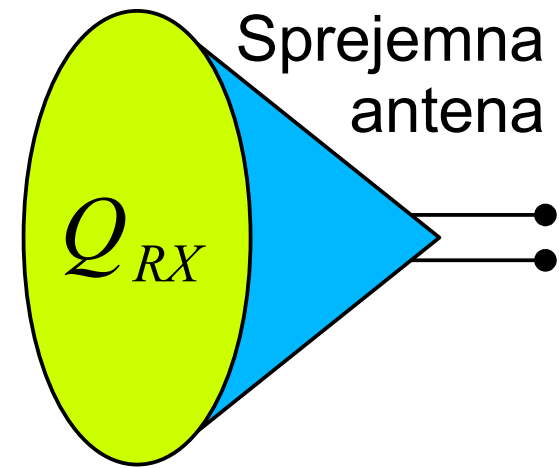
$$Q = \frac{E_L}{E_D}$$

*Osno razmerje:*

$$R = \left| \frac{1 + |Q|}{1 - |Q|} \right| \quad R_{dB} = 20 \log_{10} R$$



$$\eta = \frac{|1 + Q_{TX} Q_{RX}|^2}{(1 + |Q_{TX}|^2)(1 + |Q_{RX}|^2)}$$



Polarizacija TX		$Q_{TX}$	$R_{TX}$	Faktor skladnosti $\eta$ / polarizacija RX					
				VP	HP	RHCP	LHCP	PP <sub>45</sub>	PP <sub>135</sub>
VP	$\vec{1}_V$	1	$\infty$	1	0	1/2	1/2	1/2	1/2
HP	$\vec{1}_H$	-1	$\infty$	0	1	1/2	1/2	1/2	1/2
RHCP	$\vec{1}_D$	0	1	1/2	1/2	1	0	1/2	1/2
LHCP	$\vec{1}_L$	$\infty$	1	1/2	1/2	0	1	1/2	1/2
PP <sub>45</sub>	$(\vec{1}_V + \vec{1}_H) / \sqrt{2}$	-j	$\infty$	1/2	1/2	1/2	1/2	0	1
PP <sub>135</sub>	$(\vec{1}_V - \vec{1}_H) / \sqrt{2}$	j	$\infty$	1/2	1/2	1/2	1/2	1	0

Fraunhofer:  
daljne polje

$$\frac{E}{H} = Z_0$$

Dve polarizaciji  
 $C/B \leq 10 \text{ bit}$

MIMO:  
 $C/B \approx 20 \text{ bit}$

Fresnel:  
sevano polje

Večrodovni prenos  
 $C/B \geq 50 \text{ bit}$

$$r = \frac{2d^2}{\lambda}$$

$$r = \frac{\lambda}{2\pi}$$

Samo tu obstajajo:

$D, G,$   
 $F(\Theta, \Phi),$

Friisova enačba

Gulielmo  
Marconi

$$\frac{E}{H} \approx Z_0$$

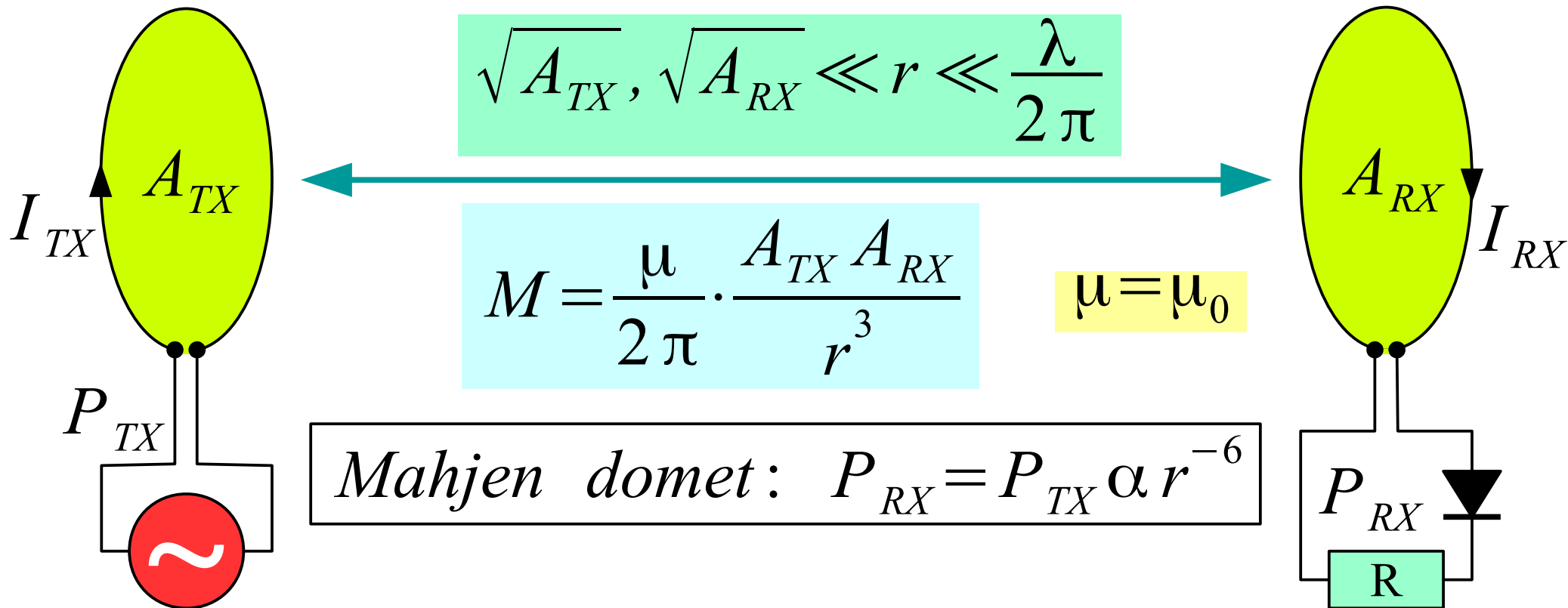
$$\frac{E}{H} \neq Z_0$$

Nikola  
Tesla

Statika:  
bližnje polje

Točkasti  
vir sevanja

$\frac{E}{H} \neq Z_0 \rightarrow$  Potrebna ločena meritev  $\vec{E}$  ter  $\vec{H}$



$\text{Re}[\vec{S}] = f(I_{TX}, I_{RX})$   
*Brez sevanja!*

Uporaba:

RFID in druge zveze kratkega dosega  
 Prenos energije (brezžično polnjenje)